

10/24/16 "Genius is 1% inspiration and 99% perspiration." -Thomas Edison

HW: Test 3 on Friday 11/4

Quarter Test on Wednesday 11/9

AIM: What are higher order derivatives?

Warm Up:

- 1) What is the rate of change of position?

Velocity

- 2) What is the rate of change of velocity?

Acceleration.

- 3) What is the rate of change of acceleration?

Jerk

Higher Order Derivatives

Did you realize that it is possible to take the derivative of a derivative? We will need this ability in the study of particle motion and objects in motion, especially related to physics in the near future.

$t = \text{time}$	$s(t)$	Position function
	$v(t) = s'(t)$	Velocity function
	$a(t) = v'(t) = s''(t)$	Acceleration function

First derivative: y' $f'(x)$ $\frac{dy}{dx}$ $\frac{d}{dx}[f(x)]$ $D_x[y]$

Second derivative: y'' $f''(x)$ $\frac{d^2 y}{dx^2}$ $\frac{d^2}{dx^2}[f(x)]$ $D_x^2[y]$

Third derivative: y''' $f'''(x)$ $\frac{d^3 y}{dx^3}$ $\frac{d^3}{dx^3}[f(x)]$ $D_x^3[y]$

Fourth derivative: $y^{(4)}$ $f^{(4)}(x)$ $\frac{d^4 y}{dx^4}$ $\frac{d^4}{dx^4}[f(x)]$ $D_x^4[y]$

EX #7: For each of the following, find the second derivative.

$$\text{A.) } f(x) = \frac{3}{2}x^3 + 5x^2 - 6x + 1$$

$$f'(x) = \frac{9}{2}x^2 + 10x - 6$$

$$f''(x) = \frac{18}{2}x + 10 = \boxed{9x + 10}$$

$$\text{B.) } g(x) = \frac{x^2 - 4x - 5}{x} = \frac{x^2}{x} - \frac{4x}{x} - \frac{5}{x} = x - 4 - 5x^{-1}$$

$$g'(x) = 1 - 0 + 5x^{-2} = 1 + 5x^{-2}$$

$$g''(x) = 0 - 10x^{-3} = \boxed{\frac{-10}{x^3}}$$

$$C.) \quad y = \frac{x}{x+2}$$

$$y' = \frac{(x+2)(1) - x(1)}{(x+2)^2} = \frac{x+2-x}{x^2+4x+4} = \frac{2}{x^2+4x+4}$$

$$y'' = \frac{(x^2+4x+4)(0) - 2(2x+4)}{(x^2+4x+4)^2} = \frac{-4x-8}{(x^2+4x+4)^2}$$

$$D.) \quad f(x) = 4\sqrt{x} - \frac{6}{\sqrt{x}}$$